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# Tachyon-Dilaton Inflation as an $\alpha'$ -non perturbative solution in first quantized String Cosmology

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# Outline

- **Motivation:** String Inflation in 4 dimensions
- Closed Bosonic String in **Graviton, Dilaton and Tachyon** Backgrounds; a **non – perturbative configuration**
- **Conformal Invariance** of this model
- **Cosmological Implications** of this model: **FRW universe & inflation** (under conditions)
- Open Issues: **Exit from the inflationary phase; reheating**

# Motivation

## Inflation:

- elegant & simple idea
- explains many cosmological observations (e.g. “horizon problem”, large - scale structure)

## Inflation in String Theory:

- effective theory
- in traditional string theories: compactification of extra dimensions of space-time is needed
- other models exist too, but no longer “simple & elegant”

# Proposal

- Closed Bosonic String
- graviton, **dilaton** and **tachyon** background
- field configuration non-perturbative in  $\alpha'$

$$\begin{aligned}g_{\mu\nu} &= \frac{A}{(X^0)^2} \eta_{\mu\nu} \\ \phi &= \phi_0 \ln \left( \frac{X^0}{\sqrt{\alpha'}} \right) \\ T &= \tau_0 \ln \left( \frac{X^0}{\sqrt{\alpha'}} \right)\end{aligned}$$

Does it satisfy conformal invariance conditions?

# Conformal properties of the configuration

General field redefinition:  $g^i \rightarrow \tilde{g}^i \equiv g^i + \delta g^i$

- Theory is invariant
- The Weyl anomaly coefficients transform:

$$\beta^i \rightarrow \tilde{\beta}^i$$

$$\tilde{\beta}^i = \beta^i + \delta g^j \frac{\delta \beta^i}{\delta g^j} - \beta^j \frac{\delta(\delta g^i)}{\delta g^j}$$

$$\left( \begin{array}{l} g^i = (g_{\mu\nu}, \phi, T) \\ \beta^i = (\beta_{\mu\nu}^g, \beta^\phi, \beta^T) \end{array} \right)$$

# Conformal properties of the configuration

- 1-loop beta-functions: homogeneous dependence on  $X^0$ , besides one term in the tachyon beta-function

$$\beta_{00}^g = -\frac{\alpha'}{(X^0)^2}(D-1+\tau_0^2)$$

$$\beta_{ij}^g = -\frac{\alpha' \delta_{ij}}{(X^0)^2}(D-1+2\phi_0)$$

$$\beta^\phi = \frac{D-26}{6} + \frac{\alpha'}{2}(D-1+2\phi_0)\frac{\phi_0}{A}$$

$$\beta^T = -2T + \frac{\alpha'}{2}(D-1+2\phi_0)\frac{\tau_0}{A}$$

- Power counting → Every other term that appears at higher loops in the beta-functions is homogeneous

# Conformal properties of the configuration

One can find a **general field redefinition**, that:

1. Doesn't change the  $X^0$  - dependence of the fields
2. Cancels the inhomogeneous term in  $\beta^T$
3. Only adds new homogeneous terms to the beta functions



$$\begin{aligned}\tilde{\beta}_{00}^g &= \frac{\tilde{E}_1}{(X^0)^2} \\ \tilde{\beta}_{ij}^g &= \frac{\tilde{E}_2}{(X^0)^2} \delta_{ij} \\ \tilde{\beta}^\phi &= \tilde{E}_3 \\ \tilde{\beta}^T &= \tilde{E}_4\end{aligned}$$

Enough freedom in the parameters of the redefinition to make the Weyl – anomaly coefficients vanish

# Conformal properties of the configuration

Analysis can be repeated order-by-order, to all orders in  $\alpha'$

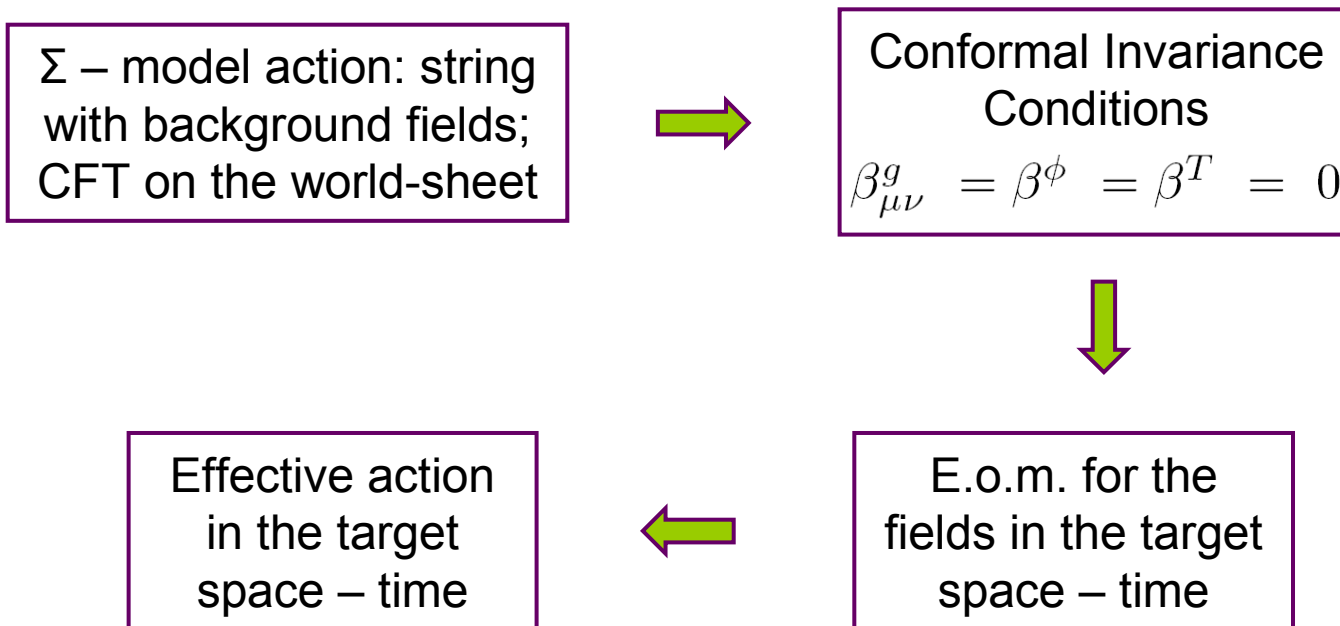


**Conformal Invariance  
to all orders in  $\alpha'$**



# Cosmology

- So far we checked that our configuration satisfies conformal invariance of the theory
- To study the cosmological implications of this model we need to study the space – time effective theory



# Effective action

“*Sigma-model frame*” (to lowest order in the derivative expansion):

$$S^\sigma = \int d^D x \sqrt{-g} e^{-2\phi} \left\{ \frac{D-26}{6\alpha'} + f_0(T) + f_1(T)R + f_2(T)\partial_\mu\phi\partial^\mu\phi \right. \\ \left. + f_3(T)\partial_\mu T\partial^\mu T + f_4(T)\partial_\mu T\partial^\mu\phi \right\}$$

$\int d^D x \sqrt{-g} e^{-2\phi} f_1(T)R$  (Einstein – Hilbert term)

need to pass to the  
“*Einstein frame*”

$$g_{\mu\nu} \rightarrow g_{\mu\nu}^E = e^{\omega(\phi, T)} g_{\mu\nu}$$

$$\omega(\phi, T) = \frac{-4\phi + 2 \ln f_1(T)}{D-2}$$

$$S^E \sim \int d^D x \sqrt{-g^E} [R^E + \dots]$$

# Sigma-model frame

metric configuration:  $g_{\mu\nu} = \frac{A}{(x^0)^2} \eta_{\mu\nu}$

$$ds^2 = \frac{A}{(x^0)^2} (dx^0)^2 - \frac{A}{(x^0)^2} \delta_{ij} dx^i dx^j$$

$$\left. \begin{aligned} y^0 &= -\sqrt{A} \ln \frac{x^0}{\sqrt{\alpha'}} \\ x^i &\rightarrow \sqrt{\frac{A}{\alpha'}} x^i \end{aligned} \right\}$$

$$ds^2 = (dy^0)^2 - e^{2y^0/\sqrt{A}} (d\mathbf{x})^2$$

$$a(y^0) = e^{y^0/\sqrt{A}}$$

$$H = \frac{1}{\sqrt{A}}$$

# Einstein Frame

$$\left\{ \begin{array}{l} ds^2 \equiv dt^2 - a^2(t) d\mathbf{r}^2 = e^\omega \left[ (dy^0)^2 - e^{2y^0/\sqrt{A}} (d\mathbf{x})^2 \right] \\ \omega(\phi, T) = \frac{-4\phi + 2 \ln f_1(T)}{D - 2} \end{array} \right.$$

Cosmology can be derived from here  $\rightarrow$   $t = t(y^0) = \dots$   
 $a(t) = \dots$

Important role:

- Form of the function  $f_1(T)$
- Form of the configuration  $\phi(y^0), T(y^0)$
- For us:  $\phi(y^0) = -\phi_1 y^0 / \sqrt{A}, \quad -T(y^0) = -\tau_1 y^0 / \sqrt{A}$

# Einstein Frame: “Eternal” Inflation

- choice for  $f_1$  :

$$f_1(T) = e^{-T}$$

$$e^{\omega} = \exp \left[ \frac{2(2\phi + T)}{2 - D} \right] = \exp \left[ \frac{2(2\phi_1 + \tau_1)}{D - 2} \frac{y^0}{\sqrt{A}} \right]$$

$$\text{If } 2\phi_1 + \tau_1 = 0$$



Einstein frame  $\equiv$   
Sigma – model frame

**Inflation**  
(in both frames)

$$a(t) = a_0 \exp \left( \frac{t}{\sqrt{A}} \right)$$

# Einstein Frame: Power-law expansion

- choice for  $f_1$  :

$$f_1(T) = e^{-T}$$

$$e^{\omega} = \exp\left[\frac{2(2\phi + T)}{2 - D}\right] = \exp\left[\frac{2(2\phi_1 + \tau_1)}{D - 2} \frac{y^0}{\sqrt{A}}\right]$$

If  $2\phi_1 + \tau_1 \neq 0$



Power-law expansion in  
the Einstein frame

$$a(t) \propto t^{1 + (\phi_1 + \tau_1/2)^{-1}}$$

$$2\phi_1 + \tau_1 > 0 \rightarrow \text{no horizons}$$

# Exit from “eternal” inflation?

Is there a way to exit from the “eternal” inflation era, and enter a power-law expansion (or even Minkowski) era?

→ Different choices for  $f_1$  will give different cosmologies

We can even find solutions in which the scale factor interpolates between an exponential and a power-law expansion

→ The condition  $2\phi_1 + \tau_1 = 0$  has to be disturbed

for example: (yet unknown) mechanism which makes the tachyon field decay to zero

# Stability of the model

Effective action in the Einstein frame:

$$\int d^D x \sqrt{-g} \left\{ R - \left[ \frac{4(D-1)}{D-2} - e^{\frac{4\phi}{D-1}} (f_1(T))^{-\frac{D}{D-2}} f_2(T) \right] \partial\phi \cdot \partial\phi \right. \\ - \left[ \frac{D-1}{D-2} \left( \frac{f_1'(T)}{f_1(T)} \right)^2 - e^{\frac{4\phi}{D-1}} (f_1(T))^{-\frac{D}{D-2}} f_3(T) \right] \partial T \cdot \partial T \\ + \left[ \frac{D-1}{D-2} \frac{4f_1'(T)}{f_1(T)} + e^{\frac{4\phi}{D-1}} (f_1(T))^{-\frac{D}{D-2}} f_4(T) \right] \partial\phi \cdot \partial T \\ \left. + e^{\frac{4\phi}{D-1}} (f_1(T))^{-\frac{D}{D-2}} \left[ \frac{D-26}{6\alpha'} + f_0(T) \right] \right\}$$

- dilaton and tachyon kinetic terms: right sign (**no ghost fields**)
- important role of  $f_1$  for vacuum energy and tachyon potential



# Summary & Conclusions

- Started from an  $\alpha'$ -non-perturbative configuration for graviton, dilaton and tachyon backgrounds of a closed bosonic String Theory
- Showed that it is consistent with conformal invariance conditions to all orders in  $\alpha'$
- Studied the Cosmological implications of this model (in the Einstein frame) and found that a de-Sitter Universe is possible
- Also found a power-law expanding universe, that can be chosen to be free of horizons

# Open Issues & Outlook

- “Eternal” inflation universe is characterized by cosmic horizons → S-matrix not well defined (problem for perturbative String Theory!)
- The dilaton-tachyon “anti-alignment” requirement spans a zero-density subspace in the space of theories. Thus, the “eternal” inflation model can be viewed as a classical model, which in String theory represents a Cosmological Constant dominating vacuum
- Exit from this classical phase? (for example: (yet unknown) mechanism which makes the tachyon field decay to zero)
- Reheating?
- Contact with phenomenology...

Thank you